

Mark Scheme (Results)

Summer 2021

Pearson Edexcel IAL In Mechanics 1
Paper WME01/01

Q	Solution	Mark	Notes
1.	\longrightarrow ku \longleftarrow 2u		
	$ \begin{pmatrix} P \\ 3m \end{pmatrix} $ $ \begin{pmatrix} Q \\ 5m \end{pmatrix} $		
	either $\longrightarrow u \longrightarrow 3u$ or $\longleftarrow u \longrightarrow 3u$		
(a)	$\pm 5m(3u-(-2u))$	M1	Use of $I = m(v - u)$ seen or
			implied, with correct terms. Condone sign errors. M0 if g included
	25 <i>mu</i>	A1	Must be positive
		(2)	
(b)	Use of CLM	M1	Or equal and opposite impulses. Requires all terms dimensionally correct. Condone sign errors.
	3mku - 10mu = 3mu + 15mu or $3mku - 10mu = -3mu + 15mu$	A1	Correct unsimplified equation for either case.
	$\Rightarrow k = \frac{28}{3} \text{or} k = \frac{22}{3}$	A1	One correct value. Any equivalent form. Accept decimal to 1dp or better.
	Equation for second value	M1	Their equation from M1 above with the final direction of <i>P</i> reversed.
	Second value correct.	A1	Any equivalent form. Accept decimal to 1dp or better.
		(5)	
		[7]	

2.	Use of $s = ut + \frac{1}{2}at^2$	M1	Form equation in <i>u</i> and <i>a</i> . N.B. Marks are available if they use two other unknowns, rather than <i>u</i> and <i>a</i>
	$20 = 3u + \frac{9a}{2}$	A1	Correct unsimplified equation
	Use of suvat	M1	Form second equation in u and a . N.B. Marks are available if they use the same two other unknowns, rather than u and a
	$10 = (u+3a) + \frac{a}{2}$ or $30 = 4u + 8a$	A1	Correct unsimplified equation
	or $30 = 4u + 8a$ $30 = 3u + \frac{21a}{2} \Rightarrow 10 = 6a, \ a = \frac{5}{3}$ $u = \frac{25}{6}$	M1	Solve for <i>u</i> or <i>a</i> Or for one of their unknowns.
	$u = \frac{25}{6}$	A1	 u and a both correct or both their unknowns correct. Accept equivalent forms. 1.7, 4.2 or better
	Use of $v = u + at$, $20 = \frac{25}{6} + \frac{5}{3}t$	M1	Complete method using <i>suvat</i> to find <i>t</i> . Correct unsimplified for their <i>u</i> , <i>a</i> .
	t = 9.5 (s)	A1	cao
		[8]	

	Allow use of column vectors		
3a	$(5i+2j)+(-3i+j)+F_3=0$ oe	M1	Use equilibrium to find \mathbf{F}_3
	$\mathbf{F}_3 = -2\mathbf{i} - 3\mathbf{j} \ (\Rightarrow a = -2, b = -3)$	A1	Correct F ₃
	$\tan\theta = \frac{2}{3}$	M1	For an equation in a relevant angle using their <i>a</i> and <i>b</i>
	$\theta = 33.7^{\circ}$	A1	34° or better. 0.588 (0.59) rads
		(4)	
3b	Resultant force = $(2 + \lambda)\mathbf{i} + (3 + 3\lambda)\mathbf{j}$	B1	Seen or implied. They must collect the i 's and j 's.
	$\mathbf{F} = 4\mathbf{a}$ oe, where \mathbf{F} is their resultant, seen or implied (could be implied by $ \mathbf{F} = 13$)	M1	Must have attempted to add all 3 forces. N.B. $3.25 = \frac{1}{4} \left[(2 + \lambda) \mathbf{i} + (3 + 3\lambda) \mathbf{j} \right]$ oe Scores B1M1M0M0A0 but allow recovery.
	Finding magnitude of their a or F $ \sqrt{\left(\frac{2+\lambda}{4}\right)^2 + \left(\frac{3+3\lambda}{4}\right)^2} \text{ or } $ $ \sqrt{\left(2+\lambda\right)^2 + \left(3+3\lambda\right)^2} $	M1	
	Use of $ \mathbf{a} = 3.25$ or $ \mathbf{F} = 13$ to form (3 term quadratic in λ) = 0 $(10\lambda^2 + 22\lambda - 156 = 0)$	M1	
	$\lambda = 3$	A1	A0 if they give 2 values.
		(5)	
		[9]	

4a	$\uparrow T - (15g + 25g) = (15 + 25) \times 0.2$	M1	All terms required. Must be in <i>T</i>	
			only.	
			Condone sign errors	
		A1	Correct unsimplified equation in <i>T</i>	
	T = 400 (N)	A1	Must be positive	
		(3)		
4b	$12g - R = -0.1 \times 12$	M1	All terms required.	
			Condone sign errors	
		A1	Correct unsimplified equation in <i>R</i>	
			only.	
			Allow $+ R$ at this stage	
	R = 119 (N) (120)	A1	Must be positive	
		(3)		
		[6]		

	Allow use of column vectors		
5a	$\mathbf{a} = \frac{(\mathbf{i} + 7\mathbf{j}) - (3\mathbf{i} + 5\mathbf{j})}{0.5} \text{ oe}$	M1	Use of $\mathbf{a} = \frac{\mathbf{v} - \mathbf{u}}{t}$ Allow \mathbf{u} and \mathbf{v} reversed
	$\mathbf{a} = -4\mathbf{i} + 4\mathbf{j}$	A1	Or equivalent
	$\Rightarrow \mathbf{v}_P = (3\mathbf{i} + 5\mathbf{j}) + (-4\mathbf{i} + 4\mathbf{j})t$	M1	For their a
	$= (3-4t)\mathbf{i} + (5+4t)\mathbf{j}$	A1ft	Follow their a . Must collect i 's and j 's This could be implied in subsequent working
	$\Rightarrow 5 + 4T = -2(3 - 4T)$	M1	Use of correct ratio to form equation in T (allow t)
	$T = \frac{11}{4}$ oe	A1	cao
		(6)	
5b	$\mathbf{v}_{p} = \mathbf{v}_{Q} \Rightarrow \begin{pmatrix} 3 - 4t \\ 5 + 4t \end{pmatrix} = \begin{pmatrix} -4 - 2t \\ \mu + 3t \end{pmatrix}$ $\Rightarrow 3 - 4t = -4 - 2t \text{and} 5 + 4t = \mu + 3t$	M1	Equate velocities and form two equations in t and μ i.e. must equate coefficients of \mathbf{i} and \mathbf{j} oe Follow their \mathbf{v}_{P}
5b		M1	equations in t and μ i.e. must equate coefficients of \mathbf{i} and \mathbf{j} oe
5b			equations in t and μ i.e. must equate coefficients of \mathbf{i} and \mathbf{j} oe Follow their \mathbf{v}_p
5b	$\Rightarrow 3 - 4t = -4 - 2t \text{and} 5 + 4t = \mu + 3t$	M1	equations in t and μ i.e. must equate coefficients of \mathbf{i} and \mathbf{j} oe Follow their \mathbf{v}_p Solve for μ . Follow their \mathbf{v}_p
5b	$\Rightarrow 3 - 4t = -4 - 2t \text{and} 5 + 4t = \mu + 3t$	M1 A1	equations in t and μ i.e. must equate coefficients of \mathbf{i} and \mathbf{j} oe Follow their \mathbf{v}_p Solve for μ . Follow their \mathbf{v}_p
5b	$\Rightarrow 3 - 4t = -4 - 2t \text{and} 5 + 4t = \mu + 3t$	M1 A1 (3)	equations in t and μ i.e. must equate coefficients of \mathbf{i} and \mathbf{j} oe Follow their \mathbf{v}_p Solve for μ . Follow their \mathbf{v}_p

6a	Resolve perpendicular to the plane	M1	Condone sin/cos confusion		
	$R = 6g\cos\theta$	A1	Correct resolution		
	$F = \frac{1}{4}R = \frac{18g}{13} = 13.6(N) \text{ or } 14(N)$	A1	2 sf or 3 sf for decimal answer		
		(3)			
6b	Equation of motion parallel to the plane	M1	Need all terms and dimensionally correct. Condone sign errors and sin/cos confusion.		
	$-F - 6g\sin\theta = 6a$	A1	Correct unsimplified equation in F Allow $-6a$ on RHS		
	$0 = 5^2 + 2 \times as$	M1	Complete method using <i>suvat</i> and calculated a ($a \neq g$) to find s		
			This is independent of previous M mark but they must have found a value for <i>a</i> .		
	$0 = 5^{2} - 2 \times \frac{8g}{13}s$ $s = 2.07(m) \text{ or } 2.1(m)$	A1	Correct unsimplified equation. Allow $(-s)$		
	s = 2.07(m) or $2.1(m)$	A1	Must be positive.		
		(5)			
6c	Equation of motion parallel to the plane	M1	Need all terms and dimensionally correct. Condone sign errors and sin/cos confusion.		
	$6g\sin\theta - F = 6a'$	A1	Correct unsimplified equation in F		
	$5^2 = 0 + 2a's$	M1	Complete method using <i>suvat</i> , with $a' \neq a$ and $a' \neq g$ to find <i>s</i>		
	$5^{2} = 0 + 2 \times \frac{2g}{13} \times s$ 8.29(m) or 8.3(m)	A1	Correct unsimplified equation		
	8.29(m) or 8.3(m)	A1			
		(5)			
		[13]			

			ATTI TOT a COTTECT
1	$M(D)$, $60g(6a-x)+Mg\times 4a = S\times 5a$ M(G), $S(x-a) = S(6a-x)+Mg(x-2a)$		A1ft for a correct
	$M(C), 60g(x-a) + Mga = S \times 5a$		terms, dim correct but condone sign errors.
	$M(B), 60g(8a-x) + Mg \times 6a = S \times 7a + S \times 2a$		For each equation, M1 for correct no. of
	$(\uparrow), 60g + Mg = S + S$ $M(A), 60gx + Mg \times 2a = S \times a + S \times 6a$	M1A1ft	unknowns (<i>M</i> and <i>S</i>) required.
, 3	Possible equations:	M1A1ft	Two equations in two
7b		(5)	
	$x = \frac{19a}{4} \text{oe}$		1
	S.C. $M(G)$, $R(x-a) = 3R(6a-x)$	M2A2	Or equivalent
	$\mathbf{SC} = \mathbf{M(C)} = \mathbf{D(c} = \mathbf{C} + \mathbf{M(C)} = $	M2A2	wrong way round1 each error
			For vertical resolution, can score M1A1, even if
			way round.
			available if using <i>R</i> and 3 <i>R</i> oe but allow if wrong
			N.B. M marks only
			clearly defined e.g. on a diagram
			unknown length which is
			could be scored for consistent use of another
			All four of these marks
			g is an A error.
			could score full marks. Inconsistent omission of
	$M(D), 60g(6a-x) = R \times 5a$		Consistent omission of <i>g</i>
	$M(C)$, $60g(x-a) = 3R \times 5a$		A1 for a correct unsimplified equation.
	$M(B), 60g(8a-x) = R \times 7a + 3R \times 2a$		condone sign errors.
	$M(A)$, $60gx = R \times a + 3R \times 6a$		M1 for correct no. of terms, dim correct but
	Possible equations:	M1A1 M1A1	Two equations required. For each equation,

8a	B A A b t		
	Correct shape for sketch for A , starting at the origin.	B1	B0 if solid vertical line at the end of either.
	Correct shape for sketch for <i>B</i> , must be correct relative to <i>A</i> , crossing it and ending at same time. Must be done on the same axes.	B1	Tram B starts later and acceleration greater.
	5, 20, 24 shown	DB1	Dependent on previous two marks
		(3)	
8b	$t = 20 + \frac{10}{3} \left(= \frac{70}{3} \right)$	B1	
	Distance travelled for either vehicle	M1	
	$\frac{1}{2} \times \frac{10}{3} \times 10$ OR $\frac{1}{2} \times 5 \times 10 + \frac{55}{3} \times 10$; $\frac{1}{2} \left(\frac{70}{3} + \frac{70}{3} - 5 \right) \times 10$	A1	
	Find second distance and subtract	M1	100 1
	$d = \frac{625}{3} - \frac{50}{3} = \frac{575}{3} = 191\frac{2}{3}$	A1	Accept 192 or better.
8c	Equate distances from O	(5) M1	Find both distances at time <i>t</i> seconds and equate, using correct structure – see examples.
	$\left(\frac{t+t-5}{2}\right) \times 10 = \left(\frac{t-20+t-24}{2}\right) \times 12$ OR $\left(\frac{1}{2} \times 5 \times 10\right) + 10(t-5) = \left(\frac{1}{2} \times 4 \times 12\right) + 12(t-24)$	A2	Correct unsimplified equation, -1 each error (up to a maximum of 2)
	t = 119.5	M1	Solve for <i>t</i>
	Distance = $5 \times (6 \times 44 - 30) = 1170 \text{ (m)}$	A1	Accept 1200 or better
		(5)	
		[13]	